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DOI: https://doi.org/10.1098/rsif.2011.0102
Emergent multicellular life cycles in filamentous bacteria due to density dependent population dynamics

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April 15, 2011

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Keywords: Generation time, life cycle, evolution of multicellularity, evolution of development

Contribution type: article
Abstract

Filamentous bacteria are the oldest and simplest multicellular life forms known. By using computer simulations and experiments that address cell division in a filamentous context, we investigate some of the ecological factors that can lead to the emergence of a multicellular life cycle in filamentous life forms. The model predicts that if cell division and death rates are dependent on the density of cells in a population, a predictable cycle between short and long filament lengths is produced. During exponential growth, there will be a predominance of multicellular filaments, while at carrying capacity the population converges to a predominance of short filaments and single cells. Model predictions are experimentally tested and confirmed in cultures of heterotrophic and phototrophic bacterial species. Furthermore, by developing a formulation of generation time in bacterial populations, it is shown that changes in generation time can alter length distributions. The theory predicts that given the same population growth curve and fitness, species with longer generation times have longer filaments during comparable population growth phases. Characterization of the environmental dependence of morphological properties such as length, and the number of cells per filament, helps in understanding the pre-existing conditions for the evolution of developmental cycles in simple multicellular organisms. Moreover, the theoretical prediction that strains with the same fitness can exhibit different lengths at comparable growth phases has important implications. It demonstrates that differences in fitness attributed to morphology are not the sole explanation for the evolution of life cycles dominated by multicellularity.
1 Introduction

Multicellularity is an organizational characteristic present in the majority of organisms whose size surpasses microbial scales. Phylogenetic inference suggests that evolutionary transitions to multicellularity have occurred several times during the history of life (Buss 1987; Bonner 1998; Carroll 2001; King 2004; Grosberg & Strathmann 2007; Rokas 2008). Nonetheless, despite its fundamental importance, it is difficult to empirically study the evolutionary and ecological forces that may lead to a transition from single-celled to multicellular organization. One set of theoretical explanations are based on examining the consequences of a shift between units of selection. These approaches consider the changing boundaries of an individual after a transition to multicellularity, and how the different activities of component cells can potentially lead to synergies that increase the fitness of the multicellular assemblage (Buss 1987; Smith & Szathmáry 1995; Michod 2000; Grosberg & Strathmann 2007). Experimental results concerning social evolution in microbes are also largely compatible with this perspective (Buss 1982; Strassmann et al. 2000; Velicer et al. 2000; Rainey & Rainey 2003; Griffin et al. 2004; Ackermann et al. 2008).

An additional set of explanations for multicellularity are based on the potential selective advantages associated with increased size. Among the proposed size-related advantages are increases in the efficiencies of feeding (Dworkin 1972; Bonner 1974; Rosenberg et al. 1977; Pfeiffer & Bonhoeffer 2003; Kreft 2004; Solari et al. 2006a; Berleman & Kirby 2009), improved dispersal (Bonner 1974; Solari et al. 2006b; Willensdorfer 2009), and predator avoidance (Stanley 1973; Guede 1979; Shikano et al. 1990; Hahn & Hoefle 1998; Pernthaler et al. 2004). Though many of the proposed explanations are highly plausible, there is a lack of empirical validation. Some notable exceptions are measurements of motility and feeding efficiencies in Volvocalean green algae (Solari et al. 2006a,b), and density dependent growth in Myxococcus xanthus (Rosenberg et al. 1977; Shapiro 1998; Berleman & Kirby 2009).
Multicellular bacteria with a filamentous form are ubiquitous in many environments, including freshwater, oceans, soil, extreme habitats and the human body (Whitton & Editors 2000; Paerl et al. 2000; Tannock 1999; Rosen et al. 2007). Extensive empirical work has been done to examine and monitor filamentous bacteria that can be toxic or problematic in the environment (Kahru et al. 1994; Sellner 1997; Ramothokang et al. 2003; Nielsen et al. 2009). Some filament-forming cyanobacteria also develop specialized terminally differentiated cells, named heterocysts, that fix nitrogen and allow for the division of labor (Stanier & Cohenbazire 1977; Wolk 1996). Though differentiation can represent a clear evolutionary advantage, theoretical and phylogenetic evidence suggests that in the cyanobacterial case, undifferentiated multicellularity evolved prior to differentiated multicellularity (Rossetti et al. 2010). In aquatic bacteria, the most common hypothesis for the advantage of filamentation—and hence undifferentiated multicellularity—is an increase in size and the concomitant defense against predation by grazers (Guede 1979; Shikano et al. 1990; Jurgens et al. 1994; Pernthaler et al. 1997; Hahn & Hoefle 1998; Pernthaler 2005). However, experiments indicate that the avoidance of predatory grazers is not the only factor causing an increased frequency of filamentous bacteria in aquatic environments (Wu et al. 2004). Notably, in some bacterial species, filament formation appears to be dependent on the growth state of the population, whereby an increase in the dilution rate of chemostat cultures leads to longer filament lengths (Hahn & Hoefle 1998; Hahn et al. 1999).

No theoretical studies address the distribution of filament lengths and the population dynamics leading to shorter or longer filaments, although differences in length can reflect the extent to which a species is able to maintain multicellularity. Environmental conditions such as temperature, solar irradiation and nutrient concentrations have been detected as factors in determining the mean size (filament length) of different cyanobacterial species.
(Kamp et al. 2008; Wu et al. 2005; Kruskopf 2006). Several of these factors also contribute to competition between species and adaptation to different niches (Lehtimaki et al. 1997; Nobel et al. 1998). Filament breakage can occur because of external mechanical stress, lytic processes initiated by pathogens (Sigee et al. 1999; van Hannen et al. 1999; Weinbauer 2004) or programmed cell death (Daft & Stewart 1973; Lewis 2000; Ning et al. 2002; Berman-Frank et al. 2004; Adamec et al. 2005).

In the present study, we deliberately avoid a modelling framework in which one assumes an a priori fitness advantage to multicellularity. We also do not aim to provide mechanistic explanations for the “origin” of multicellularity. Rather, by considering cellular growth and division in a filamentous context, we investigate the constraints that would affect filament formation and the maintenance of multicellularity. This gives an indication of the capability of bacterial organisms to evolve multicellular life cycles according to their life history traits. Our model is built on the basic assumption that the growth of a population of filamentous bacteria and the changes in length of the filaments can be set in an ecological framework. In classical population dynamics, the change in population size is governed by the processes of birth and death (and sometimes migration), combined in the well known logistic equation due to Verhulst. In this model, birth and death rates are usually assumed to be decreasing and increasing functions of the population density, respectively. When the birth and death rates are the same, the population density is at a steady state and is said to be at its carrying capacity. The value at which the two rates are equal will be here referred to as the turnover rate. The same carrying capacity can be achieved with different birth and death rate functions, and therefore at different corresponding turnover rates (Figure 1a).

Our approach to study distributions of bacterial filament length places the described density dependent concepts in the context of a population of cells that can form filamentous individuals. Although prokaryotes had been commonly thought to be in principle immortal (Williams 1957; Rose 1991), there is now evidence for programmed cell death and lysis (Rice
Bayles 2008), and in addition aging and senescence (Ackermann et al. 2003). Taking this into account, a multicellular filament is made up of several cells, and a population of filaments can be also considered as a population of cells. In this case, the population size is given by the total number of cells, while the birth and death rates coincide with the birth and death rates of each cell of the filaments. In such a population, one can vary the turnover at which a given fixed carrying capacity is achieved and ask the question if different turnovers correspond to different growth strategies; namely whether during its growth cycle the population is composed mostly of a few long filaments, or of many short filaments. Such a line of questioning is possible because as it will be shown, the rate at which a population reaches its carrying capacity can be different from the rate at which it reaches its stationary filament length distribution. The present work is an attempt to model and experimentally test the dynamics of filamentous bacteria by only considering basic life history traits of the population. The distribution of filament lengths in the different growth phases can provide insights into the developmental strategies of different filament-forming species, and the population conditions influencing multicellular development.

In the following sections, we first state the model assumptions and we specify the experimental setup for the culture of five filamentous bacterial species. Since turnover is a key factor in our model, we chose species that also exhibit different turnovers. We hence cultured heterotrophic species with fast generation time and high turnover, and photoautotrophic species characterized by a slower generation time and a low turnover. Heterotrophs differ from photoautotrophs in the way they obtain organic carbon for growth. While the former absorb organic compounds from the environment, the latter autonomously fix carbon using solar light as an energy source. We present the simulation results and test the model through a comparison with our experimental results.
2 Methods

2.1 Theoretical model

We consider a population of multicellular, undifferentiated, non-branching filamentous bacteria, whose growth is regulated only by the density-dependent birth and death rates. In this context, the total number of cells of the population is used as the population size. The birth and death rates are represented by birth and death probabilities per iteration per cell. At every iteration, each cell in a filament has a certain probability of dividing into two daughter cells or of dying. Based on these probabilities, the number of cell divisions and cell lyses are calculated in each filament. Accordingly, the filaments are elongated and then broken into smaller pieces. We simulate the change in time of the population until it has stabilized at its carrying capacity. At each iteration, the following steps are performed (see illustration § S1 of the supplementary material):

(i) Computation of the total number of cells in the population $N_c = \sum_{i=1}^{L} i n_i$, where $L$ is the maximal length of the filaments in the current generation and $n_i$ is the number of filaments of length $i$.

(ii) Computation of the birth and death probabilities per cell per iteration, corresponding to the birth and death rate functions, respectively $\beta = \beta(N_c)$ and $\delta = \delta(N_c)$:

\[
\beta(N_c) = -c_1 N_c + 1, \quad c_1 = \frac{1 - \theta}{N_c^*} \tag{1}
\]

\[
\delta(N_c) = c_2 N_c, \quad c_2 = \frac{\theta}{N_c^*} \tag{2}
\]

where $N_c$ is the total number of cells and $N_c^*$ the carrying capacity. The latter is defined as the value of the population size such that $\beta(N_c^*) = \delta(N_c^*) = \theta < 1$, where $\theta$ is the turnover. The birth rate is a decreasing function of $N_c$. The death rate is an increasing function of $N_c$. 

(iii) For each filament, we compute the number of births $b$ and number of deaths $d$ occurring in the filament. As $\beta$ and $\delta$ are the per cell probabilities, in a filament of length $i$, the total number of events $b$ or $d$ can be viewed as the number of successes in $i$ trials, each one with probability of success $\beta$ or $\delta$. By picking from a binomial distribution $B$, we determine $b$ and $d$ for each filament of length $i$:

$$b = \text{random pick from } B(i, \beta)$$
$$d = \text{random pick from } B(i, \delta).$$

The filament is elongated by $b$ cells. Then, a number of $d$ cells computed on the basis of the original filament length $i$ are randomly selected for lysis in the elongated filament. The filaments resulting from the breakages are stored for the next generation. After completing the scan of all the filaments, the new population is set for the next iteration. The choice of initial conditions and the order at which birth and death are applied to filaments do not significantly affect the results of the simulations. The default initial condition for the simulations is a single cell. Alternative algorithms implementing a reverse or a random order of birth and death steps have been tested and produced similar results (figures not shown).

As stated in point (ii), this model implements linear birth and death rate functions, with fixed carrying capacity. Alternatively, nonlinear functions have been implemented and provided qualitatively comparable results (see §S2 of the supplementary material).

Considering the difference between those rates, given by $\beta - \delta = -(c_1 + c_2) N_c + 1$, one can observe that the net growth rate $(c_1 + c_2)$ is independent of the turnover $\theta$, since $c_1 + c_2 = 1/N_c^*$. This implies that regardless of the turnover, the population size is expected to grow with the same curve for any turnover.
2.2 Relation between turnover and generation time

Before presenting the results, we provide a formula that helps to understand the connection between the model parameters and the experimental data. In the theoretical model, the turnover is the characterizing property of a strain. However, in natural bacterial populations, turnover is not an easily measurable quantity. For bacteria, doubling time during the exponential growth phase is usually calculated in lieu of generation time. Two populations with the same growth curve also have the same doubling time. Nonetheless, the reality is that the internal dynamics leading to this growth curve can vary. In the same time period, the same concentration of bacteria can be achieved by undertaking many births and deaths, or by conversely having less births and also less deaths. This leads to different turnovers and generation times. Moreover, at carrying capacity the population density is stable, hence there is no indication of generation time at that stage by measuring doubling time. Here we calculate the generation time of bacterial populations at carrying capacity in relation to turnover rate.

According to a common approach in ecology to describe the dynamics of an age-structured population (Leslie 1945), the mean age of parents at childbirth in a population with stable age distribution is calculated as:

\[
G = \frac{\left( \sum_{x=0}^{\infty} xl_x m_x \right)}{\left( \sum_{x=0}^{\infty} l_x m_x \right)}
\]

(3)

where \( x \) is the age, \( l_x \) is the probability of survival from conception to age \( x \), and \( m_x \) is the mean number of offspring at age \( x \). \( G \) can be also interpreted as a measure of generation time without making any assumption about the growth rate of the population (Charlesworth 1994). In our case, age is measured in number of iterations. We consider bacterial cells as individuals that give birth by cell division and die by a lytic process. Suppose that a cell survives a given iteration with probability \( 1 - \delta \). Then the probability
that a cell is living after \( x \) iterations if \( \delta \) remains constant is given by \( l_x = (1 - \delta)^x \). If also the probability of cell division is \( \beta \) at every iteration, the average number of offspring at a given age \( x \) coincides with the probability of birth \( \beta \), whereby \( m_x = \beta \). The generation time of a cell can then be expressed as

\[
G_{\text{cell}}(\beta, \delta) = \frac{\sum_{x=0}^{\infty} x(1 - \delta)^x \beta}{\sum_{x=0}^{\infty} (1 - \delta)^x \beta} = \frac{1 - \delta}{\delta},
\]

where the last equivalence was obtained by using geometric series. The standard formula in (3) applies when the growth rate is constant. Given the logistic nature of our model however, the functions \( \beta \) and \( \delta \) are actually dependent on the population size \( N_c \). Only when the population approaches the carrying capacity, namely when \( N_c \to N_c^* \), we have that \( \beta, \delta \to \theta \), hence the growth rate is constant (equal to 0). We then present a formula for the generation time at the carrying capacity. Substituting \( \beta = \delta = \theta \) in eq. (4), the generation time is given by

\[
G_{\text{cell}}(\theta, \theta) = \frac{1 - \theta}{\theta} \sum_{x=0}^{\infty} (1 - \theta)^x \theta
\]

which is a decreasing function of the parameter \( \theta \) (graphical illustrations in the supplementary material, Fig. S2). Hence, a population with low turnover has a long generation time, whereby cell birth and deaths occur at a low rate. On the other hand, populations with high turnover have a short generation time, whereby births and deaths occur rapidly.

### 2.3 Experimental setting

**Bacterial Strains.** The heterotrophic strains used in the experiments were *Rudanella lutea* DSM 19387\(^T\) (Weon et al. 2008) and two new bacteria isolated from a mud sample from tidal flats in Fedderwardersiel, on the North Sea coast of Germany, *Fibrella aestuarina* BUZ 2\(^T\) (Filippini et al. 2011) and strain *Fibrisoma limi* BUZ 3\(^T\) (Filippini et al., in
The autotrophic strains were two axenic cyanobacteria, *Nostoc muscorum* SAG 25.82 (identical strains ATCC 27893; PCC 7120) and *Anabaena variabilis* SAG 1403-4b (identical strains CCAP 1403/4B; UTEX 377; ATCC 29211; PCC 6309).

**Batch culture experiments for heterotrophs.** The growth of the three bacterial species was monitored in batch cultures. Stock bacteria were grown on R2A plates for 3-4 days before starting the experiment. Colonies were homogenized in 0.7% NaCl and finally distributed into 50-ml flasks containing 25 ml of SM (DSMZ 7) or R2A medium (DSMZ 830) for *F. limi*, *R. lutea* and *F. aestuarina*, respectively reaching a starting optical density (OD) of 0.04. Bacteria were grown on a shaker (120 rpm) at 29°C and after different time periods sub-samples were analyzed for OD and filament length. For *R. lutea* and *F. aestuarina*, two batch cultures (A & B) were prepared and analyzed, whereas for *F. limi* only one batch culture (A) was used for the experiment. Additionally, for each batch, three technical replicates (i.e. a1, a2, and a3) were made. The OD was measured in a spectrophotometer (SpectraMax 384 Plus, Molecular Devices, USA) at 700 and 600nm. The samples for length measurement were fixed with formaldehyde (final concentration, 2%), 20µl were distributed on a microscope slides and pictures were taken with a digital camera (Color View, Soft Imaging System, 10x, 20x and 40x objective) connected to a phase-contrast microscope (Olympus BX 51, Germany). For each time point, between 10 and 20 pictures from separate fields were taken and the sizes of the filaments were individually determined by hand using the Soft Imaging software CellF (Olympus, Germany). At least 300 filaments from 10 different pictures were counted for each time point, in order to have a representative distribution of filament lengths.

**Batch culture experiments for cyanobacteria.** As in the heterotrophic case, the growth of the two cyanobacterial species was monitored in batch cultures. Stock cultures were grown in 20 ml of BG11 medium (Rippka et al. 1979) in 50 ml Erlenmeyers one week prior to the experiment. Two ml of grown culture were added to 18 ml of BG11
Figure 1: Simulation model (a) and results based on 1000 runs (b,c,d). (a) Schematic illustration of birth and death rate functions dependent on total number of cells $N_c$. The value of the population at which the two rates are the same is defined as the carrying capacity $N_c^*$. We refer to the value of the rates at the carrying capacity as the turnover rate $\theta$. The plot illustrates that the same carrying capacity can be achieved by species that have a different turnover. (b) For all birth and death functions following the scheme in (a), $N_c$ reaches the steady state following the same growth curve despite the differing turnovers. Dashed line indicates the time at which the carrying capacity is reached (see mathematical definition of $N_c^*$ in §3.1.1). Error bars represent standard deviation of the mean. (c) When the population size reaches the carrying capacity (dashed line), the higher the turnover, the higher the total number of filaments $N_f$. Nonetheless, after many more iterations, $N_f$ reaches a steady state of about 2500 filaments for all sufficiently small turnovers (plot not shown). Error bars represent standard deviation of number of filaments. (d) Box plots of filament lengths when $N_c$ reaches the carrying capacity. Populations with low turnover have higher median length values than populations with high turnover. The corresponding pie charts on the top show the proportion of single-celled, double-celled and longer filaments in the population.
medium and cultivated on a shaker (150 rpm) at room temperature and constant light (670 lux) for three weeks. Every two days, 200 µl subsamples were taken, transferred into a microtiter plate and analyzed for OD (at 430, 630 and 680 nm; SpectraMax 384 Plus). Filament length was measured by distributing 20 µl samples in a counting chamber Neubauer-improved (Paul Marienfeld GmbH & Co, Germany) and pictures were taken with a digital camera connected to a phase-contrast microscope. Approximately 18 pictures with a 10x magnification objective (or 2 pictures with a 4x magnification objective) were taken for each time point, and the sizes of the filament were determined using the Soft Imaging software CellF. For each time point, at least 50 filaments were counted in order to have a representative distribution of filament lengths. Three experiment replicates (Erlenmeyer flasks) of each cyanobacteria and four measurement samples of each replicate were analyzed for OD. Initial stock cultures were also examined. For filament lengths, four measurement samples were assayed from a single replicate. In Figures 3d-e, we show the results of two experiment replicates (experiments A and B).

To extrapolate the cell number from the filament length, an estimated size of cells forming a filament was measured from several light microscopy pictures. From at least 60 observations, the estimated mean cell lengths are 6.0 µm, 6.7 µm and 5.9 µm for R. lutea, F. aestuarina and F. limi respectively. These values are higher than those measured from the inoculum of the same bacteria, indicating that cell size of heterotrophs may change over time. For cyanobacteria the mean cell length is less variable, and an approximate cell length of 4.0 µm was used for the conversion.
3 Results

3.1 Simulation results

3.1.1 Turnover and fitness

For the rest of this article, we will refer to the time at which the population reaches its carrying capacity as the first time $t$ such that $N_c(t + 1)/N_c(t) \leq 1 + \epsilon$, where $N_c(t)$ is the population size at time $t$ and $\epsilon = 1\%$. The growth curve of the total number of cells gives information on the fitness of the strains. Figure 1b shows that for any turnover, the total number of cells reaches the carrying capacity after less than 20 generations with the same growth curve (average and standard deviation of 1000 runs is shown). In our case, fitness is represented by net growth rate and does not depend on turnover (see §2.1).

Hence, populations with different turnovers have the same fitness. On the other hand, when the total number of cells reaches the carrying capacity, the total number of filaments ($N_f$) differs significantly according to the turnover (Figure 1c). At this point, $N_f$ ranges from values close to the carrying capacity, corresponding to almost unicellular filaments ($\theta = 0.9$), to values under 20 units ($\theta = 0.001$). Figures 1b and 1c show that the steady states of number of cells and number of filaments are not reached at the same time. This is because the stationary filament length distribution is reached much later than the steady state population density (carrying capacity). In the long run, the number of cells per filament reaches a stable equilibrium of about 2 cells per filament for sufficiently small turnovers, typically less than 0.1 (figure not shown). An analytical support for this result has been obtained by deriving an analogous model in continuous time, as presented in §S9 of the supplementary material. For higher turnovers, the effect of discretization leads to a deviation from this equilibrium. Hence, filament length distributions can be affected by turnover rates in temporary phases of the population dynamics, before a stationary distribution is reached. An example is given by the time when the carrying capacity of the
population is reached (17 iterations in this case).

3.1.2 Length distribution at the time when carrying capacity is reached

Figure 1d shows the box plot of filament lengths when the total number of cells in the population ($N_c$) has reached the carrying capacity $N_c^* = 5000$ cells. This time point however represents an intermediate stage before a stationary distribution of filament lengths is reached. The corresponding pie-charts indicate the fraction of single cells, double-celled filaments and filaments with more than two cells in the population. When turnover is close to 1 ($\theta = 0.9$), the population consists mainly of unicellular and double-celled filaments. Note that $\theta = 0.9$ means that at carrying capacity, each cell has a 90% chance of dividing as well as a 90% chance of subsequently dying. When $\theta = 0.1$, filaments with one or two cells represent about half of the population. For lower turnovers ($\theta = 0.01, 0.001$), the median values of the length are significantly higher. In the latter cases, filaments with more than two cells are more than 90%. Figure 1d shows that, as the turnover increases, the fraction of short filaments when the population reaches its carrying capacity also increases. The distribution means at this growth stage were statistically compared by means of a one-way ANOVA and a multiple comparison (see §S6 of the supplementary material). The means obtained for $\theta = 0.9$ and $\theta = 0.1$ were not significantly different. All the other pairwise comparisons were significant.

3.1.3 Length distribution during the transient phase

Figure 2 shows two examples where the mean length of the filaments was calculated every iteration. The plot shows the average of 1000 runs, with error bars indicating the 2.5th and 97.5th percentiles for the mean. The dotted line indicates the iteration at which the total number of cells reaches the carrying capacity. An increase to a peak of the mean length followed by a decay towards a steady state is observed in all cases. At the end of
the decreasing phase, the mean length is comparable to that in the beginning. The same pattern was observed also for $\theta = 0.01, 0.001$ (see § S3 of the supplementary material).

An analytical characterization of the filament length dynamics has been carried out in the supplementary material (§ S8), where an approximation for the iteration of first filament breakage has been derived. In order to statistically analyze the average length trend, we considered three reference time points and we compared the distribution of the means at those points using a nonparametric hypothesis test. As reference points we chose the starting point, the peak and the carrying capacity. The outcome of the tests provides statistical evidence of a significant increase and subsequent decrease of the average length. Details and results are given in § S6 of the supplementary material.

Significant differences are found in the maximum average length achieved. Long filaments, with a mean length up to 250 cells, are observed at a turnover of $\theta = 0.1$. Longer filaments can be achieved with lower turnovers (Fig. S4). For a higher turnover ($\theta = 0.9$), the average length of filaments at its peak does not exceed 100 cells. The observed trend indicates the prevalence of a cycle in the mean length induced by the birth and death rates, whereby filaments are short in the beginning, longer in the transient phase and again short at the carrying capacity. Moreover, in the transient phase, filaments with low turnover can elongate more than filaments with high turnover.

### 3.2 Experimental results and model validation

In the theoretical model, the population stays at the carrying capacity once this has been reached. However, since bacterial strains were not cultured in a chemostat, carrying capacities could not be maintained indefinitely. In order to assure that the experimental dataset and the simulation data are comparable, we indicate with a dotted line the time point where the bacterial populations reach their carrying capacity on each plot of the experimental results. This point was determined from the OD curves (not shown). Subsequent
Figure 2: Sample simulations showing the mean filament length along successive iterations for two different turnovers. Squares indicate the mean of the mean filament lengths obtained through 1000 runs. Edges of the error bars correspond to the 2.5th and 97.5th percentiles of the distribution of the mean filament lengths in the 1000 runs. In both cases, the mean length reaches a peak in the transient phase, and then decreases gradually toward a state comparable to the one of the beginning. Lower turnovers allow for higher transient peaks. The dotted line indicates the iteration at which the carrying capacity is reached.

In order to prove significant increase and decrease of bacterial filament length, we performed an ANOVA test associated to a multiple comparison on the data based on Tukey’s HSD test (Tukey 1949). Details of the tests for each species and within species are provided in the supplementary material (§S6).

In the following sections, the time point 0 is represented by the inoculum. The starting culture of heterotrophs was taken from plate colonies and vortexed. Because of nutrient depletion in plate colonies and mechanical breakage through vortexing, the heterotrophic inoculum is composed of mainly single cells. The starting cultures of cyanobacteria were taken from cultures grown for more than one week, gently pipetted and diluted. At inoculum, cyanobacteria filaments had an average filament length of about 45 cells (N. Muscorum) and about 75 cells (A. variabilis).
3.2.1 Mean length trend

Figures 3a, b and c show the change in time of the mean length of heterotrophic bacteria *R. lutea*, *F. limi* and *F. aestuarina*. The pattern is similar in all three cases: the mean length increases until a peak, after which it decreases and reaches a value approaching that of the inoculum (see Table S1 in the supplementary material). This trend is recognizable in Figure 4, showing micrographs of *F. aestuarina* taken at different time points. Remarkably, experiments A and B on *F. aestuarina* give very similar results, showing a high repeatability of the observed pattern (Fig. 3c). A comparison of the theoretical and *F. aestuarina* length distributions against time is shown in the supplementary material (§S4, Figure S6). The mean length of cyanobacteria, tracked for two months, shows a qualitative trend similar to that of heterotrophs, albeit much slower. Both the *A. variabilis* and *N. muscorum* species have a mean-length peak in the transient phase. However, because of the low turnover, they need more time than heterotrophs to reach the stationary distribution, as predicted by the model. When they reach carrying capacity, they are still long.

The pattern observed in heterotrophs is comparable with the simulation results shown in Figure 2. The trend of the cyanobacteria, although not so markedly conclusive, gives indication that the model predictions hold also in autotrophs. An additional illustration of the mean length trend of the cultured species is provided in Figure S5 of the Supplementary Material.

3.2.2 Length in the transient phase

Generation times in heterotrophs and cyanobacteria are very different. While the former are observed on the scale of hours, the latter grow on a scale of days/weeks. The difference could be in principle due to the different trophic state of the bacteria. This hypothesis could be tested by means of a comparison between different generation times intraspecifically in the autotrophs or in the heterotrophs. However, this goes beyond the scope of
**HETEROTROPHS**

- **a) R. lutea**
  - Mean filament length (μm) vs. time (hours)
- **b) F. limi**
  - Mean filament length (# cells) vs. time (hours)
- **c) F. aestuarina**
  - Mean filament length (μm) vs. time (hours)
- **d) N. muscorum**
  - Mean filament length (# cells) vs. time (days)
- **e) A. variabilis**
  - Mean filament length (μm) vs. time (days)

**CYANOBACTERIA**

- **d) N. muscorum**
  - Mean filament length (# cells) vs. time (days)

**HETEROTROPHS AND CYANOBACTERIA**

- **f) Distribution of filament lengths when reaching carrying capacity**

**Figure 3:** (a)-(e) Empirical measurements showing mean length of bacteria against time. Edges of the error bars correspond to the 2.5th and 97.5th percentiles of the measured lengths. Diamonds indicate the mean of measured filament length at each time point. Data from both heterotrophic and photoautotrophic species are shown. The zero time point corresponds to the inoculum. The dotted line indicates the time at which the carrying capacity was reached. (f) Box plots of filament lengths when the bacterial populations reach their carrying capacity. The capital letter next to the species name indicates the experiment used in the plot. The corresponding pie charts on the top indicate the proportion of single-celled, two-celled and longer filaments in the population.
the present work and we proceed relying on the mathematical derivation of section § 2.2. According to the relation between generation time and turnover established in § 2.2, we assume that the heterotrophs and cyanobacteria have high and low turnovers, respectively. The simulation results presented in § 3.1.3 show that the peak value of the mean length in the transient phase increases with decreasing turnover. Figure 3 shows that heterotrophic filaments will rarely be longer than 60 cells. The length of cyanobacteria can be significantly higher than that of heterotrophs. *N. muscorum* and *A. variabilis* filaments have up to around 350 and 600 cells respectively. Hence, cultured bacterial populations support the model predictions, indicating that bacteria with a putatively higher turnover (in this case heterotrophic species) are able to elongate less than those with lower turnover (cyanobacteria).

### 3.2.3 Distribution of lengths at the time when carrying capacity is reached

In Figure 3f, the box plots and the pie charts show the proportion of short and long filaments in the cultured bacterial populations when they reach their carrying capacity. As for the simulation results, the pie charts illustrate three length classes, namely single cells, double-celled filaments and filaments with more than two cells. The heterotrophs show a considerable amount of short filaments, with a proportion of single cells and double-celled filaments varying across species in the range 8%-16% and 29%-42% respectively. In cyanobacteria, filaments with one or two cells are absent. Figure 3f can be compared with Figure 1d. Again, the experimental results confirm the theoretical predictions, according to which short filaments at the carrying capacity are more abundant in populations with high turnover.
Figure 4: Bright field micrographs of *F. aestuarina* bacteria at different stages of their growth. The initial population (inoculum) is composed of many small filaments. After 17 hours, the filaments reach their maximal length. After this peak, the bacteria progressively break towards a mixed population of short and medium filaments as they reach their carrying capacity (48 hours). Eventually, the filament lengths approach the mean of the inoculum.
Figure 5: Simulations and experiment of serial transfers. Symbol shapes and shading indicate different transfers. Arrows indicate the trend of each culture. (a) Computer simulations of successive transfers. When the average filament length is at its peak, the population density is below the carrying capacity. Whenever a culture reaches this peak, the corresponding average length is used as a starting condition of a new simulation at lower density (transfers 1 to 4). This procedure simulates the transfer of an aliquot of a higher density population to a fresh medium. Edges of the error bars correspond to the 2.5th and 97.5th percentiles of the distribution of the mean filament lengths in the 1000 runs. (b) Average length of *F. aestuarina* during serial transfers to fresh medium. The first transfer was done after 17 hours. For the first five transferred cultures, the mean length was measured and plotted at several successive time points. For subsequent cultures, only one measurement was taken. Edges of the error bars correspond to the 2.5th and 97.5th percentiles of the measured lengths.
3.2.4 Serial transfer experiment and simulations

If filament elongation is governed by density dependent processes as hypothesized in the model in §2.1, then interventions on such underlying processes should produce testable hypotheses. Experimental manipulation of cell densities is one simple possibility. If the population drops significantly below its carrying capacity, the filaments that survive in this new condition should be able to elongate or at least maintain their original length until the carrying capacity is reached again. We simulated and experimentally carried out a series of successive transfers of bacterial populations, whereby a fraction of the population was transferred to a fresh medium whenever the average length of the original population was close to its peak. Filaments developing in the fresh medium were expected to keep or increase the length reached at the previous stage. Details of the computational and experimental settings are provided in §S7 of the supplementary material. Figure 5a shows the average length of filaments obtained by successive transfer simulations. Figure 5b shows the average length of *F. aestuarina* tracked along successive transfers. In this case, filament size slightly increases or remains almost constant in most of the cases. The fact that filaments do not elongate so strongly as in the simulations could be due to physical handling (breakage of long filaments while pipetting) or to other culture conditions influencing the elongation that were not considered in the model. The model results indicate that the filaments transferred to the fresh medium maintain or increase their length, and eventually, start shortening when they reach their carrying capacity again. The experimental results, although not as strong as the simulations, show that the transferred bacteria are generally able to maintain their length.
4 Discussion

Filamentous bacteria can be viewed as a simple example of multicellular individuals. Some of them, such as filamentous cyanobacteria, have been present in the environment since the early stages of life, as indicated by fossil records and phylogenetic analyses (Hofmann 1976; Amard & Bertrand-Sarfati 1997; Westall et al. 2006; Schirrmeister et al. 2011). The theoretical model shows that at various life stages, two populations with the same fitness and carrying capacity can differ in the composition of filament length classes according to the life history traits regulating their growth. Although the long term stationary distribution of filament length is the same for any sufficiently small turnover rate, the differences due to turnover observed at other growth stages (e.g. transient phase, when reaching carrying capacity) are quantitatively significant and biologically relevant. Filaments belonging to a population with high turnover (and hence short generation time) have moderate lengths at their maximum growth phase. Furthermore, when the population reaches carrying capacity, they are chiefly unicellular. Individuals of a population with low turnover (and hence long generation time) can instead become very long in the transient phase, and still be multicellular when reaching the carrying capacity. The species that we cultured show evidence that the predictions of the model hold. The relation between bacterial generation time and turnover derived in §2.2 helps us to understand the relationship between simulations and experiments. The heterotrophs have a faster generation time than the cyanobacteria (and hence a higher turnover). As a consequence, while the heterotrophic filaments are rarely longer than 60 cells, the cyanobacteria can reach lengths of up to 600 cells. Theory and experiments both show that according to different life history traits, bacteria can cover a wide spectrum of lengths, indicating that multicellularity can be achieved to different degrees. Moreover, a key feature of this model is that the predominance of multicellularity during the life cycle is not necessarily determined by morphology-dependent differences in
fitness. Here, the factors affecting multicellularity are birth and death rates, and hence
turnover rate and generation time.

The model indicates a common temporal behaviour for filament length distributions.
The mean length increases and peaks during the transient growth phase, and then decreases
until it reaches a value approaching the initial conditions. The results from cultured bact-
erial populations of heterotrophic and photoautotrophic species show that the predicted
trend in filament length distribution is robust across species, and is representative of what
occurs in nature. The fact that individuals eventually become shorter (and of average
length 2 at the stationary distribution) regardless of turnover is due to the effect of cell
lysis on a filament. Consider a filament of length $L$. A cell division (birth) increases its
length by one unit, namely the filament length becomes $L + 1$. By contrast, after a cell
lysis, the expected filament length will be on average $L/2$. The average effect of cell death
on length is hence much larger than that of cell birth. This is consistent with the expecta-
tion that the average filament length in a population can keep increasing if the death rate
remains sufficiently low, as shown in the estimation of the time of first filament split (§ 8 of
the supplementary material). When the average filament length in the population is at its
stationary distribution, cell birth and death have the same effect. This is achievable only
if the filaments are of average length 2. This argument is supported by the analysis of the
analogous continuous time model derived in the supplementary material. In this context,
a way to avoid the breakage into small filaments is to decrease the effect of cell lysis on
organism size. A solution in this direction is the evolution of a second or third dimension,
as in spherical multicellular bacteria (Keim et al. 2004) or microbial biofilms. In this cases,
if we think of a square or a ball of $N$ cells, a cell division will still lead to an individual
of $N + 1$ cells, but cell death will also only decrease size by one unit, resulting in a size of
$N − 1$ (as opposed to $N/2$).

There are no previous theoretical and experimental results that are directly comparable
to the results presented here. However, the extensive work of Hahn & Hoefle (1998) and
Hahn et al. (1999) set important precedents and reference points. These works focus on the
effects of predators on selection for longer filament lengths. Their results are not directly
comparable to those presented here because the death rates due to predators preferentially
afflict smaller filaments and single cells. However, they also provide revealing information
on the dynamics of filament formation in the absence of predators. Hahn et al. (1999)
show that increasing the nutrient flow and the dilution rate of a chemostat in the absence
of predators leads to longer filament lengths. This corresponds to our prediction that in
transient growth conditions with lower population densities, filament lengths would get
longer. Furthermore, though they do not present extensive data on this, Hahn et al.
(1999, p.28) mention that in batch culture, the percentage of multicellular filaments is
higher in the exponential phase in comparison to the stationary phase. This situation is
again consistent with the predictions presented here.

The model studied here is a general model of filamentous growth, and is not restricted
to prokaryotes. Many simple forms of eukaryotic algae grow in a multicellular filamen-
tous form, and the theoretical results presented here are in principle also valid for such
eukaryotes. However, it is clear that eukaryotic algae have surpassed their prokaryotic
counterparts in their morphological diversity. There are at least six major algal lineages
in which filamentous multicellularity has evolved: the Phaeophyta, Rhodophyta, Chrys-
ophyta, Chlorophyta, Charophyta and Embryophyta (Niklas 2000). However, in each of
the latter cases, higher dimensional variants have also evolved, whereupon cell division
can occur in more than one planar dimension. This diversity can for example range from
the simple globular multicellularity of some of the Volvocales (within the Chlorophyta),
to the highly differentiated and developmentally complex vascular land plants (within the
Embryophyta). Furthermore, plants can differentiate into diverse developmental modules
such as branching nodes, leaves, inflorescences, and root structures. By combining such
modules in different combinations, they can access a wider variety of morphologies during their growth process (Prusinkiewicz & Lindenmayer 1990; Sultan 2000). This flexibility in morphology can translate into both phenotypic plasticity and evolvability.

Developmental life cycles are not unique to multicellular eukaryotes, and an understanding of how they evolved is lacking. Theory and experiments in this article indicate that the size of the individual, in terms of number of cells, can follow a cycle: from unicellular (or short length) to multicellular and back to unicellular (or short length) again. Each time, the initiation of the cycle can be hypothetically achieved by moving cell density below the carrying capacity (e.g., increases in fluid or nutrient availability). The transfer experiment and simulations do not contradict this hypothesis.

In our model, only the birth and death rates play a role in the change in size during the bacterial life cycle. These life history traits are intrinsic properties of every living organism. This pattern, which automatically arises from the interplay between ecology and the filamentous nature of the bacteria, is an emergent property. As such, it can serve as the basis for a primitive life cycle, upon which a more complex developmental program can be subsequently built. As a case in point, some species of Nostoc can differentiate into hormogonia during low growth phases characterized by high stress or scarce resources. These hormogonia are short filaments specialized for survival in harsh conditions, which subsequently migrate to a new area before growing into full grown filaments again (Meeks & Elhai 2002). Our results suggest that the cycling of filament lengths between growth and static phases of the population is a pre-existing context within which multicellular developmental cycles and differentiation can evolve.
References


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