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Emerging cell array based on reaction–diffusion

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Abstract This article demonstrates the self-replication and self-organization phenomena based on a reaction–diffusion mechanism by computer simulation. The simulation model consists of a one-dimensional cell array. Each cell contains two kinds of chemical substances, activator u and inhibitor v , that can generate a reaction–diffusion wave, which is a spatial concentration pattern. The cells are supposed to be divided or deleted depending on the concentrations of chemical substances. We tried several kinds of diffusion coefficient in the model, and in some simulations, a self-replication process and a generating cell array with a metabolic process were observed. By applying the division rule and the apoptosis rule, cell arrays duplicate in two oscillating states, i.e., self-replication processes were observed. By applying a division rule and an annihilation rule, a cell array that has a stable length is generated by changing the cell components, i.e., generating a cell array by a metabolic process was observed. Surprisingly, these two phenomena are realized independently of the initial number of cells.

Key words Reaction · Diffusion · Morphogenesis

Introduction

The self-replication and self-organization abilities of multicellular organisms are among the most fundamental characteristics that discriminate creatures from non-creatures. As each cell contains the same genome, this feat is realized in a distributed and autonomous way in the absence of central-

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ized control. However, in spite of the great progress that has been made in molecular biology over the past few decades, the overall picture of the principles behind the spatiotemporal dynamics of these processes is still lacking. In 1952, A.M. Turing advocated a reaction–diffusion mechanism, and suggested that this mechanism, which is a kind of spatial concentration pattern, plays a key role in forming a periodic shape in a small creature called a hydra.¹ L. Wolpert² suggested a concept of positional information because he thought that cells need to recognize themselves by their position because they all have identical genes. C.G. Langton built a cellular automata model of self-replication (SRloops) on a two-dimensional cell array. As the model consists of discrete internal states with finite state automata, it is not easy to relate this model to the biological cell. K. Tomita et al.⁴ created graph automata, which gave a description of the dynamic topological change in a cell network. They extended the concept of cellular automata to certain graphs of cells. This model is able to describe morphological changes such as cell division or cell death, but little attention has been given to a relation between morphogenetic processes and a reaction–diffusion mechanism.

Model

Reaction–diffusion

In this research, a one-dimensional cell array model was chosen for simplicity. Figure 1 shows a schema of the model. These nodes represent cells containing two kinds of chemical substance, activator u and inhibitor v , that can generate a reaction–diffusion wave. These two chemicals react with each other and diffuse into neighboring cells according to the concentration gradient.

$$du_r/dt = +5u_r(t) - 6v_r(t) + 1 + D_u \{u_{r-1}(t) + u_{r+1}(t) - 2u_r(t)\} \quad (1)$$

$$dv_r/dt = +6u_r(t) - 7v_r + 1 + D_v \{v_{r-1}(t) + v_{r+1}(t) - 2v_r(t)\} \quad (2)$$

The reaction–diffusion model that we use is the same as Turing's, which is expressed as partial differential Eqs. 1

Fig. 1. One-dimensional cell array

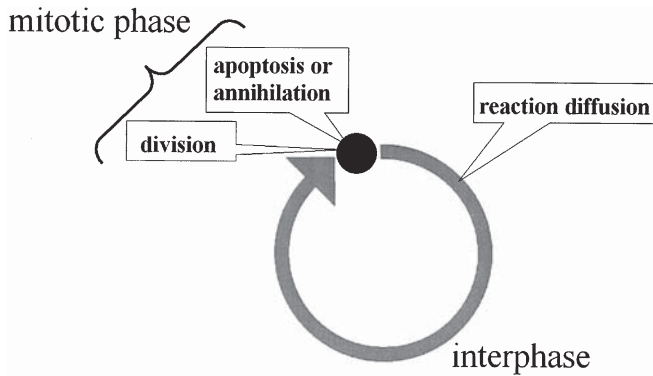
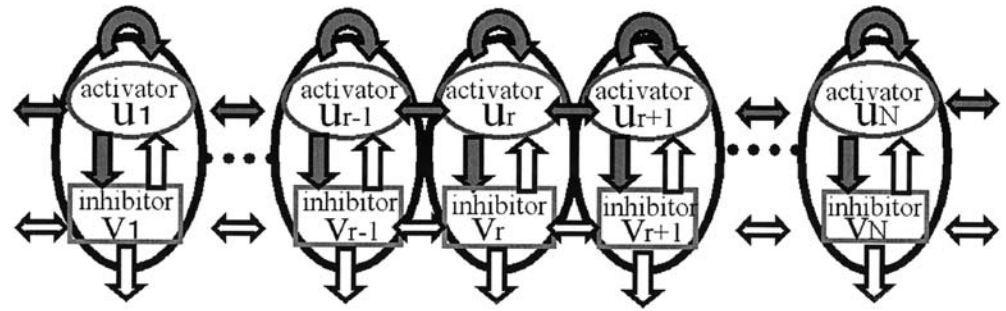


Fig. 2. Cell cycle

and 2, where u_r and v_r represents the concentration of activator and inhibitor, respectively, with subscript r as an identification number. D_u and D_v represent the diffusion constants of the activator and inhibitor, respectively ($D_u = 0.7$, $D_v = 1.2$). Dirichlet boundary conditions were applied to the system, which set the chemical concentration at the boundary to zero. The initial concentrations were set as the equilibrium point $(u, v) = (1.0, 1.0)$.

Cell cycle and cell differentiation

Since the cell cycle is determined by various factors, in this article the cell cycle is supposed to be generated synchronously. Figure 2 represents the cell cycle in the model. Every cell has an interphase and a mitotic phase in the cycle. In the mitotic phase, reaction and diffusion of the chemical substances take place. In the interphase, cells are differentiated depending on the chemical concentrations (see below).

Figure 3 shows the cell differentiation rules. Cell division (top) takes place when the concentration of the activator becomes greater than a specific threshold (the division threshold, set as 1.5) in the mitotic phase. The cell divides into two cells, and the concentration of each chemical substance immediately before division is their concentration in each divided cell.

Conversely, the annihilation rule (middle) is activated when the concentration of the activator becomes lower than another specific threshold (the annihilation threshold, set as 1.0) in the mitotic phase. In this rule, one cell is deleted, but the connection of the other two cells remains. The apoptosis rule (bottom) is similar to the annihilation rule, and is acti-

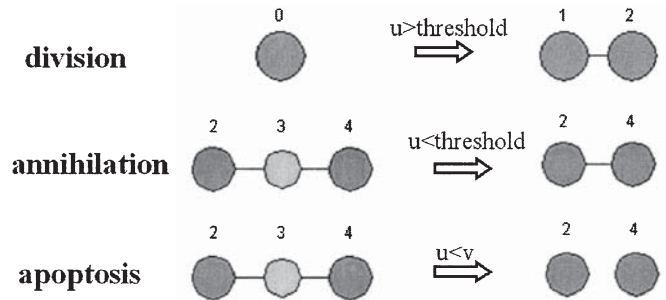


Fig. 3. Cell differentiation

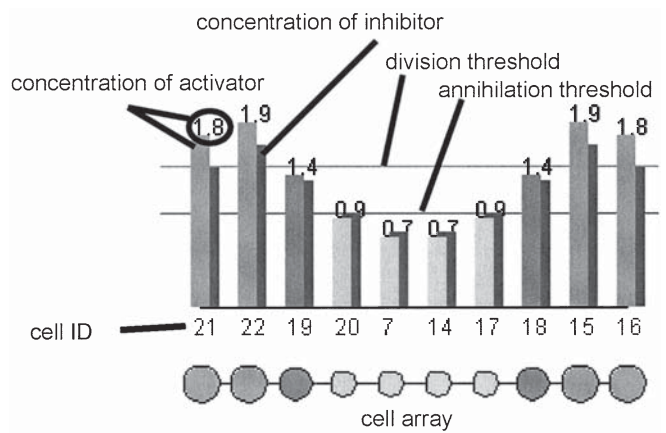


Fig. 4. Simulation model

vated when the concentration of the activator becomes smaller than that of the inhibitor in the same phase. The system is then divided into two separate groups by cell deletion. Every differential equation is integrated by the Runge–Kutta method ($\Delta t = 0.01$, 1 step = 100 Δt , 1 interphase corresponds to 150 steps).

Simulations and results

In the computer simulations, eqs. 1 and 2 and the cell differentiation rules are simulated synchronously according to the cell cycle. Figure 4 shows the simulation model. The bars above each cell represent the concentrations of activator and inhibitor. The concentrations of the activator are displayed in front, and those of the inhibitor are displayed behind. The values of the concentrations of the activator are

Fig. 5. A self-replication process in one cell

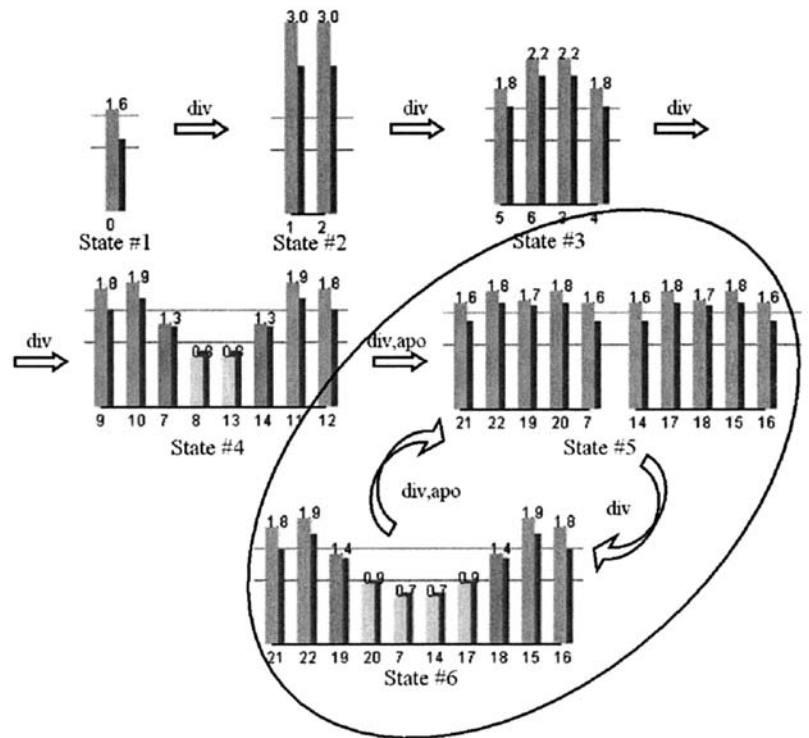
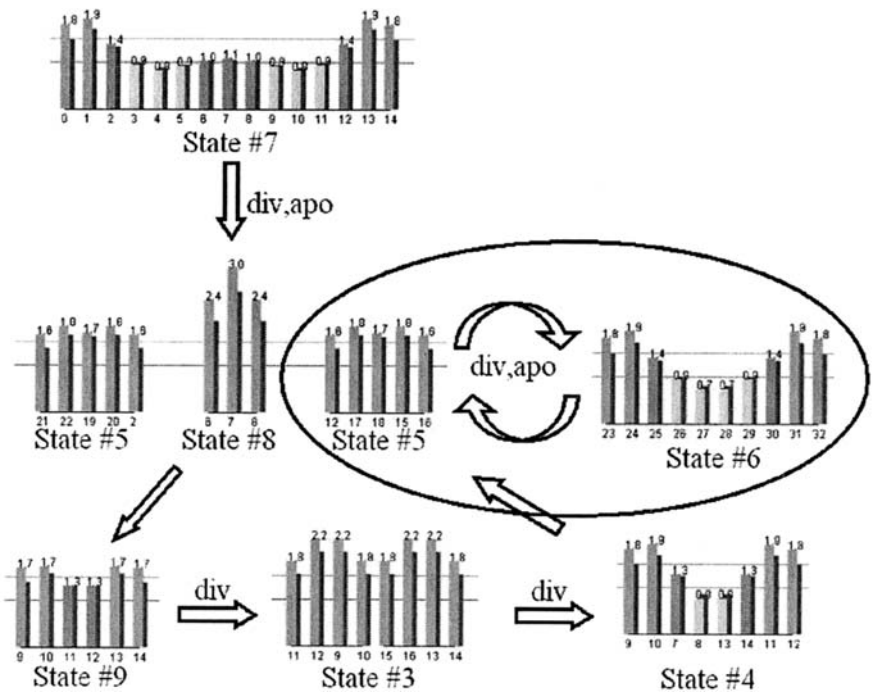


Fig. 6. A self-replication process from 15 cells



presented on each shoulder of the bar. The division threshold, annihilation threshold, and identification numbers of the cells are also listed.

Self-replication process

In this model, the division rule and the apoptosis rule are applied in the mitotic phase. Figure 5 shows the self-replication process when we settled on one cell as the initial condition. In the first stage, cell divisions are repeated twice

in the mitotic phase, and the initial cell grows into 8 cells (state 1 to state 4). Then the apoptosis rule is activated, four cells positioned at the center (cells 8 and 13 in state 4) are deleted, and four cells at the side (cells 9–12 in state 4) are divided. Consequently, the system duplicates itself by oscillating between state 5 and state 6.

Figure 6 shows the case where the initial number of cells is larger than the oscillating number 10 (state 7). The phenomenon that the final state converges to states 5 and 6 is observed.

Fig. 7. A cell array generating by a metabolic process from one cell

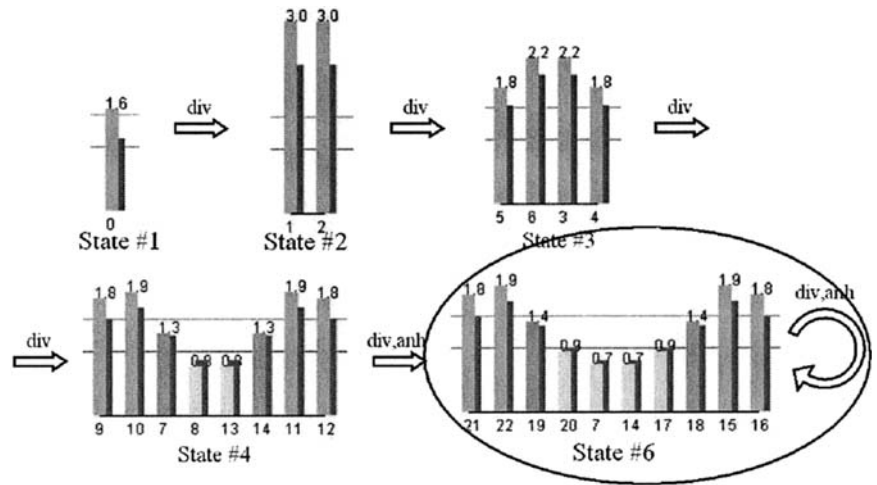
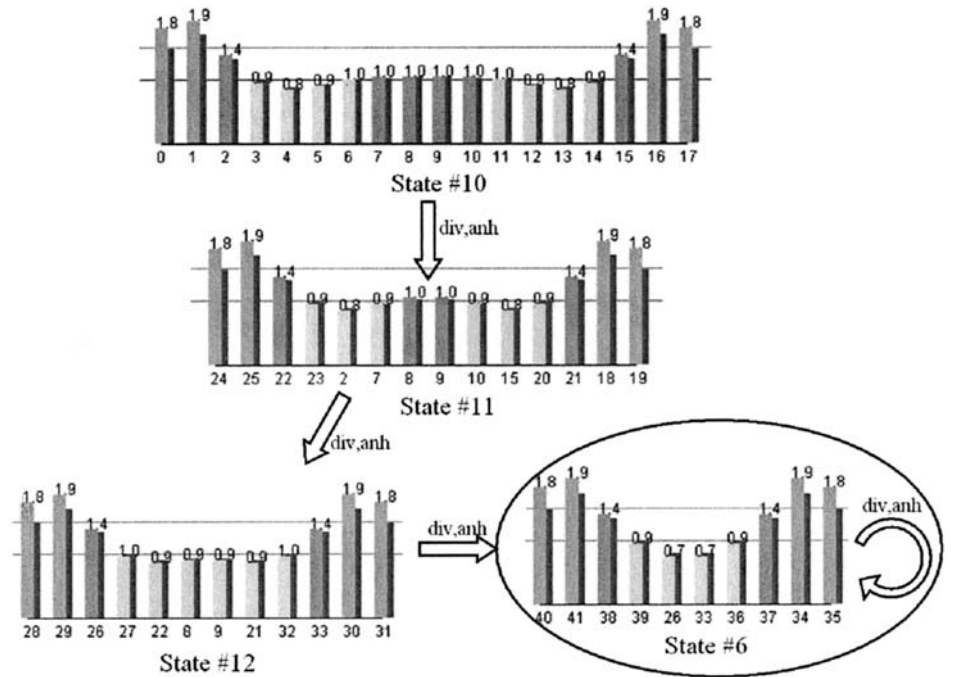


Fig. 8. Generating a cell array from 18 cells



Generating a cell array with a metabolic process

The division rule and the annihilation rule are applied in the mitotic phase. Figure 7 shows that the number of cells increases to 10 according to the cell division rule. In the mitotic phase at state 6, four cells positioned at the center (cells 20,7,14 and 17 in state 6) are annihilated, and another four cells (cells 21,22,15, and 16) at the sides are divided. Finally, the number of cells remains stable at 10. The system perpetually produces new cells and replaces some old cells.

In order to investigate the stability of the process, 18 cells are set in the initial state. Figure 8 shows that the number of cells finally converges to the same pattern (state 6).

Discussion

In addition to the simulation described above, we chose different numbers of cells as the initial condition, and the results are shown in Fig. 9. The X-axis represents the number of mitotic phases passed and the Y-axis represents the number of cells. This figure shows that the length of all cell arrays which start from between 1 cell and 30 cells finally converge to 10. This suggests not only that we can choose variable numbers of cells for an initial condition (at least from 1 to 30), but also that we can cut any cell connections, but we will still generate two cell arrays of size 10.

Since the patterns of reaction–diffusion waves seem to be unique to the length of the cell arrays, especially when the length is short, we counted the number of cells which exceeded the division threshold but which were below the

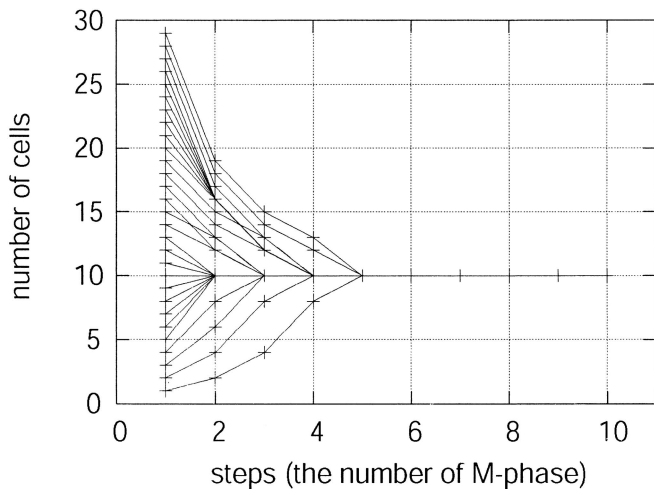


Fig. 9. Transition graph of the number of cells

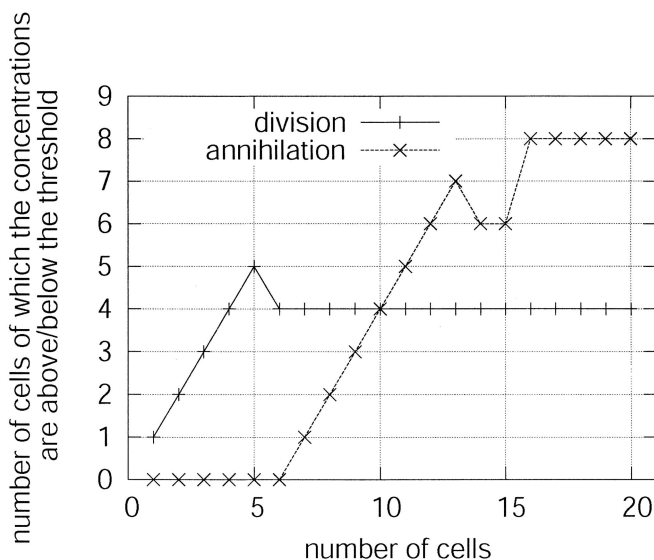


Fig. 10. Graph when the threshold is exceeded

annihilation threshold in the first mitotic phase. The X -axis in Fig. 10 represents the number of cells, and the Y -axis represents the number of cells in which the concentrations are above (or below) the threshold. As the figure shows, when the number of cells is less than 9, the number of cells that exceed the division threshold is larger than the numbers which are below the annihilation threshold. That is, the length becomes short in the next mitotic phase, and when the number of cells we choose is more than 11, the result is the other way round. This figure clearly shows that the system converges to 10.

Figure 11 represents the number of cells when the mitotic phase has passed ten times with different diffusion coefficients. The initial number of cells was between 1 and 30 for each parameter set. The X and Y axes represent the diffusion coefficients D_u and D_v , respectively, and the Z axis represents the number of cells. As can be seen, the system does not always converge to one state, and although the

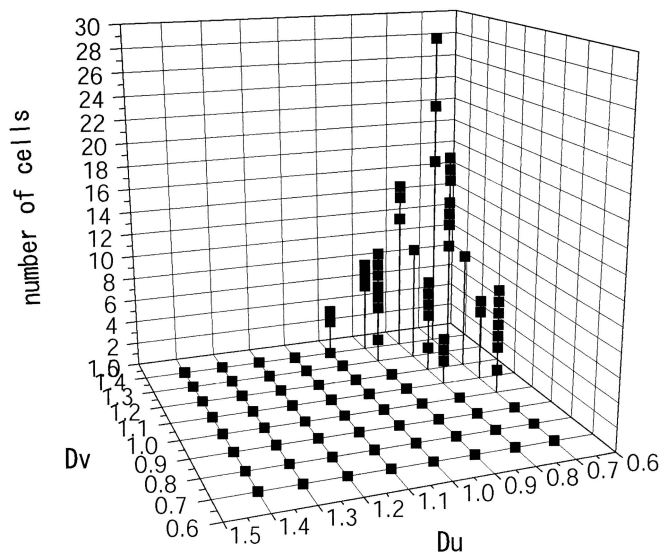


Fig. 11. The number of cells in each parameter set

system shows its robustness in the event of external disturbances by its adequate diffusion coefficients, the ranges of these parameters are narrow.

Conclusion

In conclusion, two fundamental organic behaviors, i.e., the self-replication process and generating a cell array by a metabolic process, were observed by applying a reaction-diffusion mechanism on distributed space. In the self-replication process, the phenomenon that cell arrays duplicate themselves by oscillating between two states was observed. In generating a cell array by a metabolic process, the phenomenon that a cell array which has a stable length is generated by changing its cell components was observed. This research shows the possibility that a reaction-diffusion system plays some role in controlling these vital activities of living things.

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