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Jet cross sections at the LHC with NNLOJET

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We review the status of NNLO calculations for jet cross sections at the LHC. In particular, we describe how perturbative stability and convergence can be used as criteria to select the most appropriate scales in the theoretical description of di-jet and single jet inclusive production.

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1. Introduction

Due to their large production rate, low-multiplicity jet cross sections are among the best-measured collider observables. At the LHC, they are measured differentially in the jet kinematics with an accuracy often reaching the percent level [1, 2, 3, 4, 5, 6]. Combined with perturbative QCD predictions of comparable accuracy, these precision data have the potential to determine fundamental parameters of the Standard Model with percent level errors and to constrain beyond Standard Model physics searches. Those accurate measurements also provide an ideal ground for probing the perturbative behaviour of QCD predictions computed at a given order in the strong coupling α_s .

Theoretical predictions for hadron collider observables are built from two main constituents: the parton-level cross sections and the parton distribution functions. These predictions have two types of uncertainties: parametric and perturbative. The parametric uncertainties arise from the ingredients to the predictions that cannot be computed from first principles, but are extracted from data: α_s and the parton distributions. They both depend on auxiliary scales: the renormalization scale (μ_R) and the mass factorization scale (μ_F).

The perturbative uncertainty, which is our main concern here, arises from the truncation of the perturbative series and is most often quantified by varying the renormalisation and factorisation scales around some predefined common central value, referred to as central reference scale. This commonly used procedure provides an estimation of the theoretical uncertainty related to the unknown missing higher orders terms in the theoretical predictions. The choice of this central scale, although usually physically motivated, is arbitrary: any suitable choice is a priori equally valid.

Up to now, jet observables have been compared to data at NLO level only [7, 8, 9]. Most recently, di-jet [10] and single jet inclusive [11] production cross sections and related distributions have been computed to NNLO in QCD, including all partonic channels, but restricting the NNLO corrections to the numerically dominant leading colour and leading N_F terms.

These computations were performed using the NNLOJET framework, which is a parton-level event generator including all partonic channels relevant at a given order, and which provides the full kinematical information on all final state particles. The NNLOJET framework is a common infrastructure used to compute NNLO corrections for jet production processes, employing the antenna subtraction method [12, 13] to capture all infrared divergencies from the corresponding matrix elements. A detailed description of the NNLOJET framework including the specific processes which have been implemented in this infrastructure up to now, can be found in [14].

These NNLO calculations, as they include the knowledge of three orders in the perturbative expansion in α_s provide a unique opportunity to test expectations regarding the perturbative convergence and stability of theoretical predictions when higher order corrections are included in the computation of these observables.

It was furthermore observed that at NNLO, different, but equally motivated choices of the central scale value resulted in substantially different predictions for jet observables yielding a significant perturbative uncertainty and preventing so far the use of jet data in PDF fits, see [15].

It is the purpose of this talk to present detailed studies on the impact of choosing a particular functional form for the central scales in di-jet and single jet inclusive production.

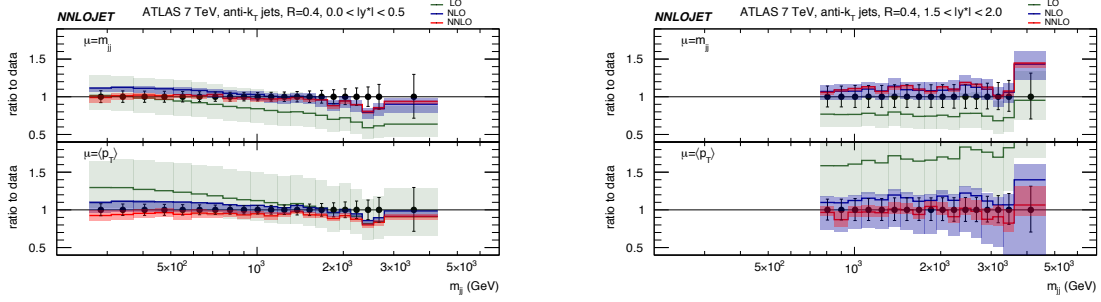


Figure 1: Ratio of theory predictions to data for $0.0 < |y^*| < 0.5$ (left) and $1.5 < |y^*| < 2.0$ (right) for the scale choices $\mu = m_{jj}$ (top) and $\mu = \langle p_T \rangle$ (bottom) at LO (green), NLO (blue) and NNLO (red). Scale bands represent variation of the cross section by varying the scales independently by factors of 2 and 0.5.

2. The di-jet production cross section

Di-jet observables are defined through the two jets with the largest transverse momentum in the event. In [10] we have presented the NNLO calculation of di-jet production doubly differential in the invariant mass m_{jj} and half of the absolute rapidity difference of the two leading jets, ($|y^*| = |y_{j1} - y_{j2}|/2$) and compared it to the available ATLAS data [1] at 7 TeV. This comparison was performed using the following central scale choices: the invariant mass m_{jj} and the average transverse momentum of the two leading jets, $\langle p_T \rangle$.

At NLO, it was previously noted that the predictions obtained with these two central scale choices are substantially different. This observation raised doubts on the reliability of the perturbative description of di-jet production, and the corresponding data were often not included in global determinations of parton distributions. Including the NNLO corrections, this spread in the predictions is reduced substantially, as can be seen in Fig.1. The spread is rapidity dependent, and some impact of the central scale choice is still observed in the rapidity region $1.5 < |y^*| < 2.0$, while being largely absent at low rapidity separation. While the spread is reduced considerably at NNLO, yielding mutually compatible predictions, the two central scale choices display a considerably different perturbative convergence and residual scale uncertainty. This leads us to conclude that the scale choice $\mu = m_{jj}$ appears to be the most appropriate in the theoretical description of the di-jet cross section.

With this choice as reference central scale, when comparing our NNLO predictions for the double differential cross section with the ATLAS data at 7 TeV [1], we found that those predictions yield a good agreement in shape and normalization with the data for all the kinematical range in invariant mass and rapidity. The inclusion of NNLO corrections leads to a significant improvement in the description of the data even for the low invariant mass and rapidity range where the NLO prediction deviated from it. It is also found that the residual scale uncertainty at NNLO is smaller than the experimental uncertainty for this observable.

These findings regarding the scale sensitivity in the di-jet observables cannot be transferred straightforwardly to the single jet inclusive production cross section, as we will see below.

3. The single jet inclusive production cross section

The single jet inclusive production cross section is obtained by summing over all reconstructed jets in an event. By ordering the jets in transverse momentum, this cross section can be expressed as the sum of the jet cross sections for the first (leading), second, third (and so on) jets in the event. It has been studied extensively by the ATLAS and CMS collaborations [1, 2, 3, 4, 5, 6] as a function of the transverse momentum p_T and rapidity y at various center-of-mass energies ranging from $\sqrt{s} = 7$ TeV to $\sqrt{s} = 13$ TeV.

Beyond the requirement of observing at least one jet, no further constraints on the final state particles are imposed on this observable. As a consequence, an event can contain multiple jets and all jets that pass the jet fiducial cuts contribute individually to the cross section. Unlike in di-jet production where in a given distribution each event is counted once in a given kinematical bin, for the single jet inclusive production cross section, a single event can have multiple entries in the binned histogram.

The phenomenological analysis of single jet inclusive processes thus turns out to be much more involved than in the di-jet production case. The fact that the contributions to inclusive distributions come from individual jets rather than events introduces more possibilities for the choice of the central scale in the theoretical predictions. We investigated this in detail in [16], considering the following options (and multiples thereof):

- the individual jet transverse momentum p_T
- the leading-jet transverse momentum $p_{T,1}$
- the scalar sum of the transverse momenta of all partons \hat{H}_T

We can distinguish two generic categories classifying these functional forms: jet-based (p_T) or event-based ($p_{T,1}$, \hat{H}_T). In the first case, in a given event, the scale used for the individual jet contributions is different for each jet while for an event-based scale prediction, a common scale is used for all jets in the event.

For a given fixed value of the central scale, the theoretical predictions for single jet inclusive observables, depend on the kinematics of the reconstructed jets, in particular on the jet cuts and the radius of the jet cone size R used in the jet algorithm. The main difference between predictions obtained with different scale choices arise from events which are not in the Born $2 \rightarrow 2$ back-to-back kinematical configuration. In this back-to-back kinematical situation, which is also reached at high p_T , those scales ($p_T, p_{T,1}, \hat{H}_T$), or multiples of these, are equivalent and using any of them yields the same predictions.

Away from these back-to-back configurations, the scales differ and besides the dominant leading jet contribution, the effect of the sub-leading jet contributions become sizeable. As a consequence, the impact of changing the scales becomes more and more important as the size of the jet cone R decreases, where the importance of the sub-leading jet contributions is enhanced. To demonstrate this effect, we focus on two cone sizes $R = 0.4$ and $R = 0.7$, as used by the LHC experimental collaborations.

Up to now, the most commonly used scale choices in describing single jet inclusive observables were p_T and $p_{T,1}$. In [17], we showed that the NNLO predictions for these two scale choices

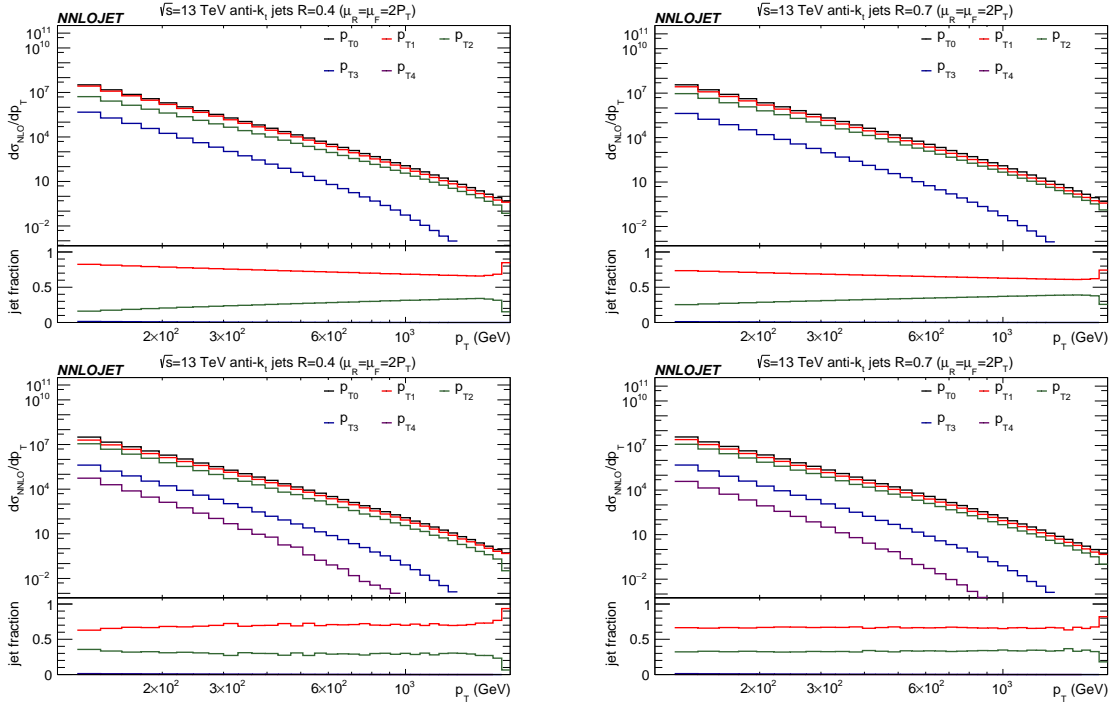


Figure 2: Breakdown of the single jet inclusive cross section integrated over rapidity into contributions from first, second, third and fourth jet at NLO (upper plots) NNLO (lower plots) evaluated for $\mu = 2p_T$ for the jet cone sizes (left) $R = 0.4$ and (right) $R = 0.7$.

differ substantially. While at high p_T , a clear trend showing a stabilisation and agreement of the predictions is manifest, at low p_T , significant differences between the predictions persist and are even more pronounced at NNLO. This unexpected behaviour motivated the further study presented in [16], where the different ingredients to single jet inclusive distributions were analysed according to their behaviour at higher orders in the perturbative expansion.

It is worth mentioning that when decomposing the inclusive jet cross section in leading and sub-leading jet contributions, the individual jet distributions are well-defined and infrared safe only if they are inclusive in the jet rapidity. This is related to the fact that the rapidity assignment is not well-defined for the leading order kinematics where the transverse momentum of first and second jets are identical. When higher orders corrections are included, this can result in situations where the role of leading and sub-leading jet is interchanged between event and counter-event, thereby hampering their cancellation in infrared limits. In the inclusive jet transverse momentum distribution, this problem does not happen as all jets are summed over.

In order to be able to select the most appropriate scales for the theoretical description of the single jet inclusive production process, we define a list of desired properties, that a central scale choice should satisfy in order to produce reliable predictions for single jet inclusive observables. A detailed analysis of the leading and sub-leading jet distributions (in the context of a thorough comparison of p_T and $p_{T,1}$, see [16]) showed that some central scale choices lead to infrared sensitive predictions with pathological behaviours regarding perturbative convergence and stability. It was found that the second jet distribution is particularly sensitive to the scale choice, sometimes even

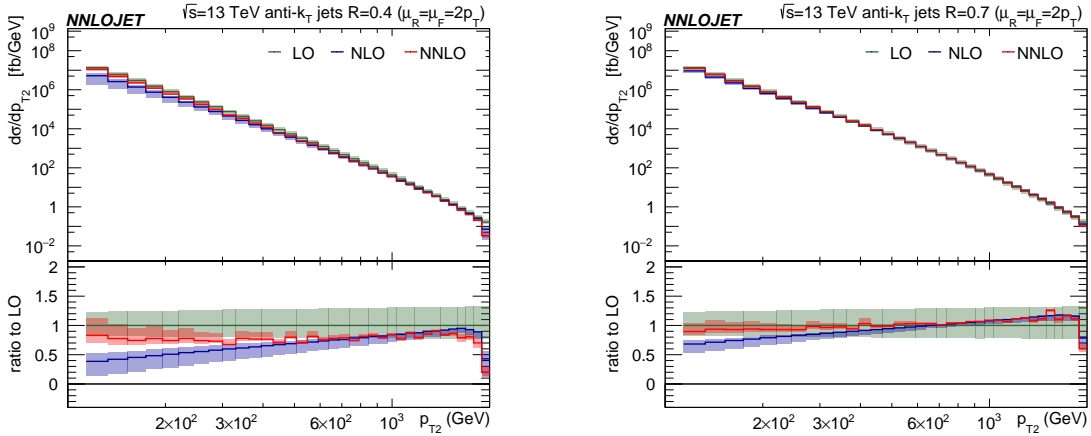


Figure 3: Perturbative corrections to the transverse momentum distribution of the second jet at 13 TeV (CMS cuts, $|y| < 4.7$, $R = 0.4$ (left) and $R = 0.7$ (right)), integrated over rapidity and normalised to the LO prediction for the central scale choice $\mu = 2p_T$. Shaded bands represent the theory uncertainty due to the variation of the factorization and renormalization scales.

exhibiting an unphysical behaviour in predicting negative cross sections.

We therefore identify a set of requirements that a central scale choice should fulfil, prior to any comparison with experimental data. These are: (a) *perturbative convergence*, (b) *scale uncertainty as error estimate*, (c) *perturbative convergence of the individual jet spectra*, (d) *stability of the second jet distribution*.

While the first two criteria are rather standard requirements, and have been used to select m_{jj} as best choice for the central reference scale in di-jet production, the latter two criteria are specific to the single jet inclusive production and in particular to the single jet inclusive transverse momentum distribution.

Using our selection procedure on the transverse momentum distributions integrated over rapidity and employing the CMS kinematical set-up [6] to define the final state jets, we were able to identify $\mu = 2p_T$ and $\mu = \hat{H}_T$ as the two theoretically best-motivated scale choices for single jet inclusive production. Note that the former belongs to the class of jet-based scales, the latter is an event-based scale and that the two scales coincide in Born kinematics.

In what follows, we present the most compelling features leading to this selection outcome for one of the selected central scale choices: $\mu = 2p_T$. We start by presenting the breakdown of the single jet inclusive transverse momentum distribution into leading and sub-leading jet fractions. In Fig. 2, we see that over most of the p_T range at NNLO, the leading jet contribution dominates, while the second jet fraction is sizeable and the third and fourth jet fractions are completely negligible for both cone sizes. At NLO, the second jet contribution becomes less and less important as p_T decreases. Going to NNLO, we observe a substantial increase in the second jet fraction compared to the NLO case specially at low p_T , the largest difference being observed for the smaller cone size $R = 0.4$.

Given the potentially larger impact on the inclusive jet cross section of the second jet p_T distribution at NNLO, as compared to NLO, we analysed its perturbative stability in further detail [16]. In Fig. 3, we observe that for $\mu = 2p_T$, this distribution exhibits stable higher order corrections

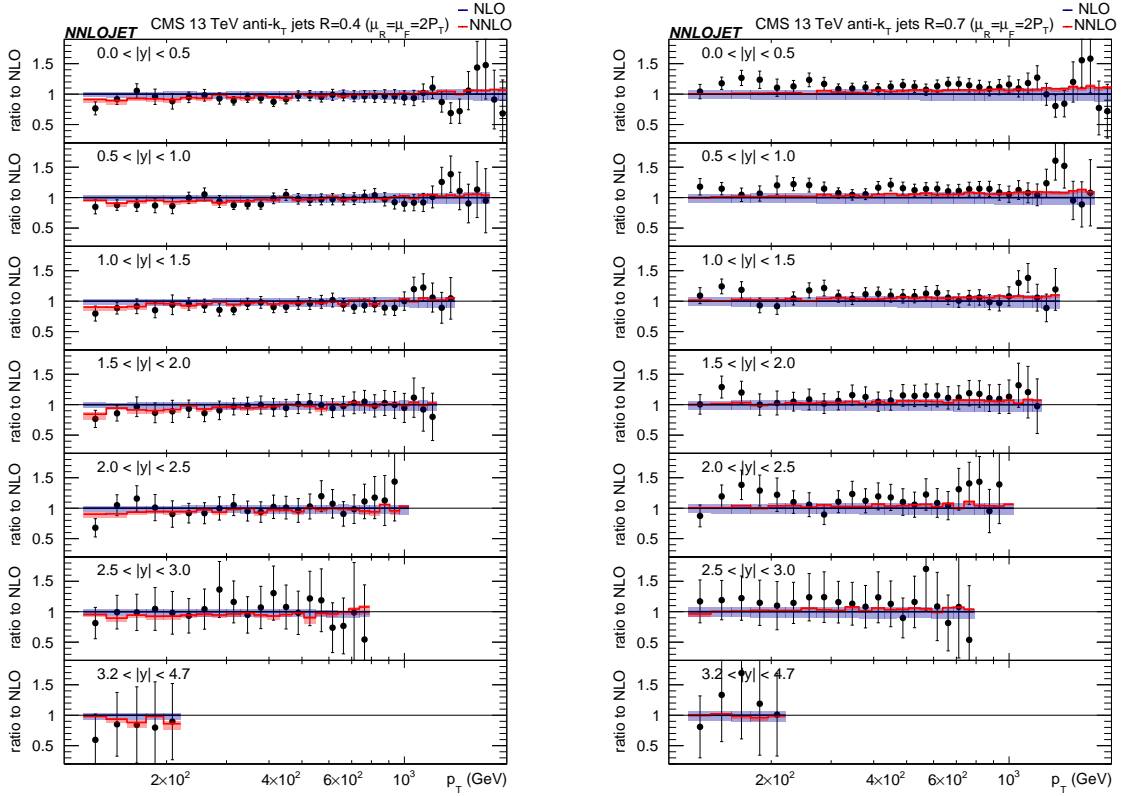


Figure 4: Double-differential single jet inclusive cross sections measurement by CMS [6] and NNLO perturbative QCD predictions as a function of the jet p_T in slices of rapidity, for anti- k_T jets with $R = 0.4$ (left) and $R = 0.7$ (right) normalised to the NLO result $\mu = 2p_T$. The shaded bands represent the scale uncertainty.

and small residual NNLO uncertainties while being positive over the whole p_T range for both cone sizes. For most of the other central scale choices considered, these specific distributions yielded unphysical negative predictions.

In [16], the optimal scale choices $\mu = 2p_T$ and $\mu = \hat{H}_T$, have been validated further by studying the distributions of the single jet cross section differential in transverse momentum and also in rapidity. Furthermore, for these scale choices, a direct comparison for the double-differential single jet inclusive cross-sections to the CMS available data [6] at $\sqrt{s} = 13$ TeV has been performed. As seen in Fig. 4 for $\mu = 2p_T$, we observe small positive NNLO corrections across all rapidity slices, that improve the agreement with the CMS data, as compared to the NLO prediction for both cone sizes. In addition, across the entire p_T range, a clear reduction of the scale uncertainty is manifest when going from NLO to NNLO.

4. Conclusions and outlook

In this talk, we have highlighted the main outcomes of recent studies regarding the choice of a reference central scale for the factorisation and renormalisation scales in observables related to the di-jet and single jet inclusive production processes [10, 16]. We have emphasized the substantial

differences between the perturbative behaviour of their differential cross sections. While in the di-jet case, the knowledge of the NNLO corrections was sufficient to establish m_{jj} as the preferred choice based on standard perturbative convergence and stability criteria, we saw that in the case of the p_T spectrum in single jet inclusive production a more elaborated list of requirements is needed to identify $\mu = 2p_T$ and $\mu = \hat{H}_T$ as the most appropriate from a list of a priori equally valid and reasonable scale choices. We saw in particular that $\mu = 2p_T$ fulfils the selection criteria associated to the second jet contribution, whose impact in the single jet inclusive cross section is particularly sensitive to the instabilities. Using these theoretically well-motivated scale choices, the NNLO predictions for di-jet invariant mass and single jet p_T distribution are in good agreement with the data presenting a significant reduction of the scale uncertainty over most of the allowed kinematical range in m_{jj} and p_T respectively. We expect that these results will enable precision phenomenology with jet data, such as the NNLO determination of the parton distributions functions and of fundamental QCD parameters.

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